

Modified Enlarged 24pt
OXFORD CAMBRIDGE AND RSA EXAMINATIONS

Tuesday 5 November 2019 – Morning

GCSE (9–1) Mathematics

J560/04 Paper 4 (Higher Tier)

**Time allowed: 1 hour 30 minutes
plus your additional time allowance**

YOU MUST HAVE:

Insert for Question 7

YOU MAY USE:

a scientific or graphical calculator

geometrical instruments

tracing paper

A model for question 18

Please write clearly in black ink.

Centre number

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Candidate number

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First name(s) _____

Last name _____

READ INSTRUCTIONS OVERLEAF



INSTRUCTIONS

Use black ink. You may use an HB pencil for graphs and diagrams.

Answer ALL the questions.

Read each question carefully before you start to write your answer.

Where appropriate, your answers should be supported with working. Marks may be given for a correct method even if the answer is incorrect.

Write your answer to each question in the space provided.

If additional space is required, use the lined page(s) at the end of this booklet. The question number(s) must be clearly shown.

INFORMATION

The total mark for this paper is 100.

The marks for each question are shown in brackets [].

Use the π button on your calculator or take π to be 3.142 unless the question says otherwise.

Answer ALL the questions.

- 1 Carol makes birthday cards.
Each card takes the same amount of
time to make.**

**She makes 3 cards in 48 minutes.
She has an order for 80 cards.**

**Can she complete this order in 3 days if
she works 8 hours each day?
Show how you decide.**

_____ because _____
_____ [5]

2 Use the formula $F = \frac{s}{\sqrt{tm}}$ to find the value of F when

$$s = 5.8 \times 10^6$$

$$t = 4.1 \times 10^8$$

$$m = 3.7 \times 10^{-2}.$$

Give your answer in standard form, correct to 2 significant figures.

[4]

- 3 At a railway station, trains are either eastbound or westbound.
An eastbound train leaves the station every 25 minutes.
A westbound train leaves the station every 45 minutes.**

An eastbound train and a westbound train both leave the station at 8 am.

When is the next time that two trains leave the station together?

[4]

- 4 Bob makes dry concrete by mixing cement, sand and stone in the ratio 1 : 2 : 3 by weight. He buys the cement, sand and stone in bags as shown in this table.**

	Weight of bag (kg)	Cost per bag (£)
Cement	25	5.50
Sand	20	2.00
Stone	15	3.90

He packs the dry concrete into 30 kg bags.

Bob buys just enough cement, sand and stone to make 50 bags of dry concrete.

**(a) Show that Bob buys 500 kg of sand.
Use the space below. [3]**

(b) Bob sells the 50 bags of dry concrete for a total of £396.

Calculate Bob's percentage profit.

(b) _____ % [5]

5 Multiply out and simplify.

$$(4x + y)(x - 3y)$$

[3]

- 6 A bag of sweets contains only mints, sherberts and toffees.**

The ratio of the number of mints to sherberts is 2 : 3.

The ratio of the number of sherberts to toffees is 7 : 5.

What fraction of the sweets are sherberts?

[3]

- 7 12 students take two tests.
Each test is out of 60.
The scatter diagram on the insert
shows the results for 10 of the
students.**

- (a) The table shows the results for the
other 2 students.**

Test 1	36	38
Test 2	44	41

**Plot these results on the scatter
diagram. [1]**

- (b) Describe the type of correlation
shown in the scatter diagram.**

(b) _____ [1]

(c) (i) Draw a line of best fit on the scatter diagram. [1]

**(ii) Another student was absent for Test 2.
The student scored 40 marks on Test 1.**

Use your line of best fit to estimate a result for this student on Test 2.

(c)(ii) _____ [1]

**(d) Work out the percentage of THE
12 STUDENTS whose result on
Test 1 is LOWER than their result on
Test 2.**

(d) _____ % [4]

- 8 The diagrams show the price paid by two groups of people visiting a funfair.

5 adults	£	
4 children	£	
Total		£ 78

3 adults	£	
6 children	£	
Total		£ 63

Assume each adult pays the same price and each child pays the same price.

Find the price for an adult and the price for a child.

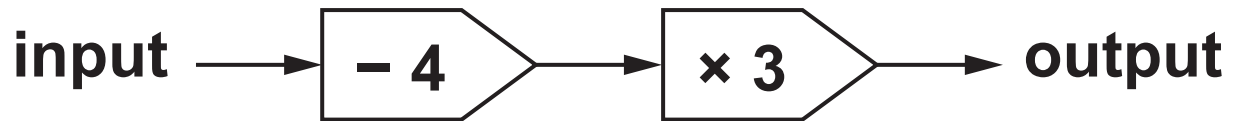
Adult price = £ _____

Child price = £ _____

[5]

9 Here is function A.

Function A :



- (a) A number, k , is input into function A.
The output is also k .

Find the value of k .

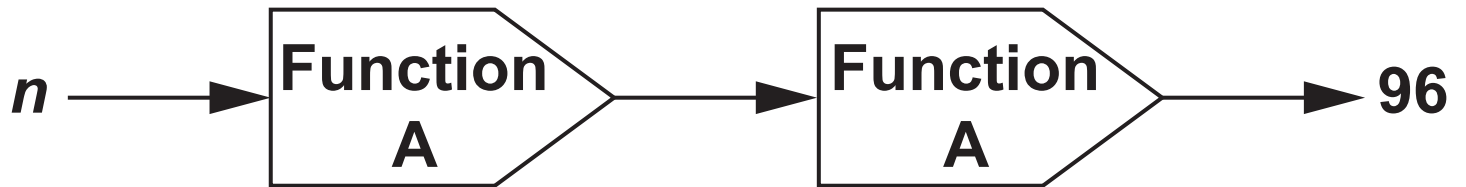
(a) $k =$ _____ [3]

(b) The output of function A is y .

**Write an algebraic expression,
in terms of y , for the input of
function A.**

(b) _____ [2]

- (c) The diagram shows a composite function with an input, n , and an output of 96.



Find the value of n .

(c) $n =$ _____ [2]

10 The value of a house, £ H , is given by the formula

$$H = 165\,000 \times 1.03^t$$

where t is the number of years after 1st January 2010.

(a) Write down the value of the house on 1st January 2010.

(a) £ _____ [1]

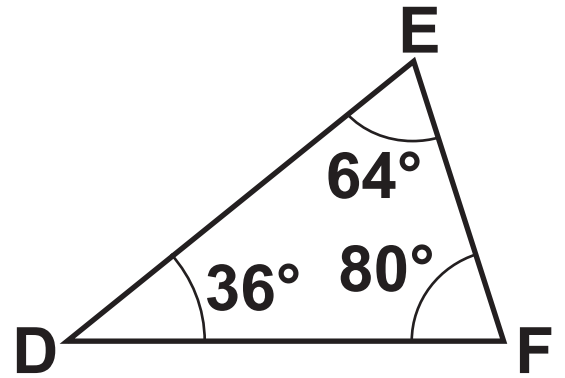
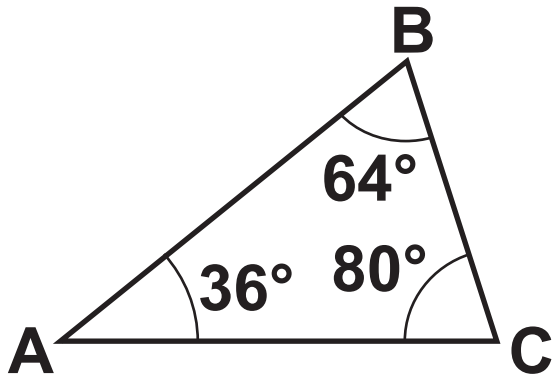
(b) Write down the annual percentage increase in the value of the house.

(b) _____ % [1]

(c) Show that the value of the house is over £200 000 on 1st January 2017. Use the space below. [2]

- 11 (a) Are these two triangles definitely congruent?
Give a reason.

NOT TO SCALE

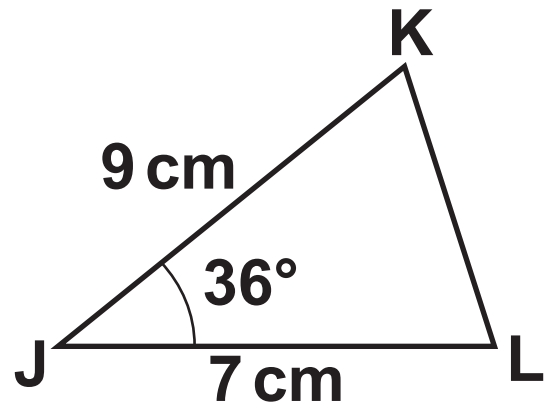
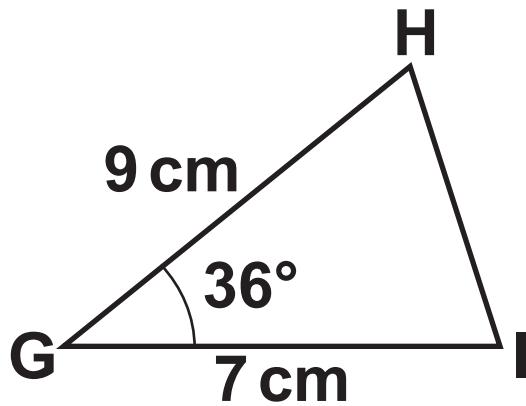


_____ because _____

_____ [1]

(b) Prove that these two triangles are congruent.

NOT TO SCALE



[3]

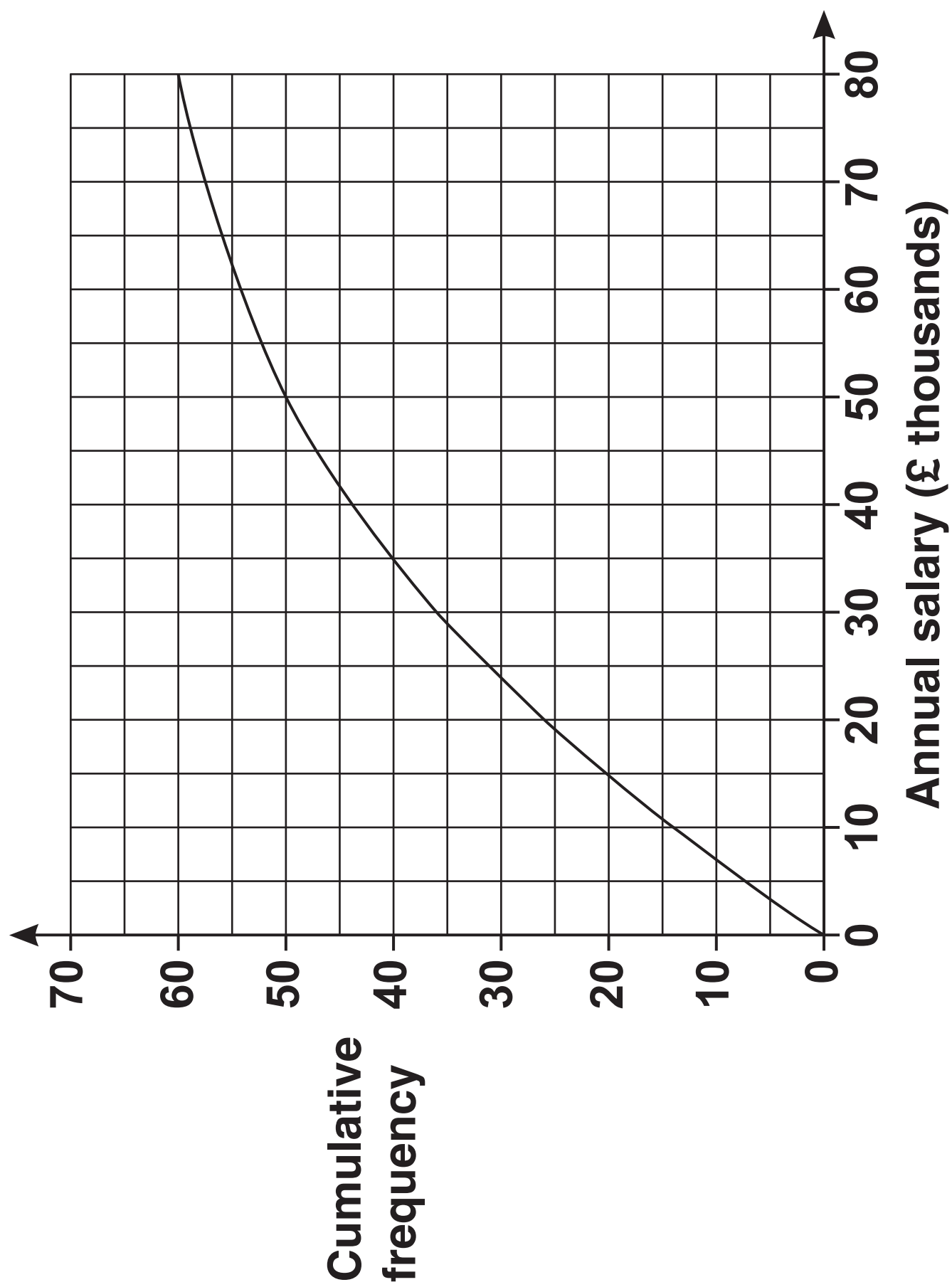
12 The cumulative frequency graph opposite summarises the annual salary, p (£ thousands), of the 60 workers in a factory.

(a) Use the graph to estimate the median annual salary.

(a) £ _____ thousands [1]

(b) Complete this cumulative frequency table. [2]

Annual salary, p (£ thousands)	Cumulative frequency
$p \leq 10$	
$p \leq 20$	
$p \leq 30$	
$p \leq 50$	
$p \leq 80$	



(c) Use the information in the cumulative frequency table to calculate an estimate of the mean annual salary.

(c) £ _____ thousands [5]

(d) Explain why your estimate of the median is more reliable than your estimate of the mean.

_____ [1]

- 13 (a) A transport lorry consists of a cab and a trailer.
The trailer has a volume of 90 m^3 .
Alfie makes a model of this lorry using a scale of 1 : 72.**

Work out the volume of the trailer in Alfie's model, giving your answer in cm^3 .

(a) _____ cm^3 [3]

**(b) Alfie paints his model lorry.
He has eight colours available.**

He decides to paint the cab in one colour and the trailer in a different colour.

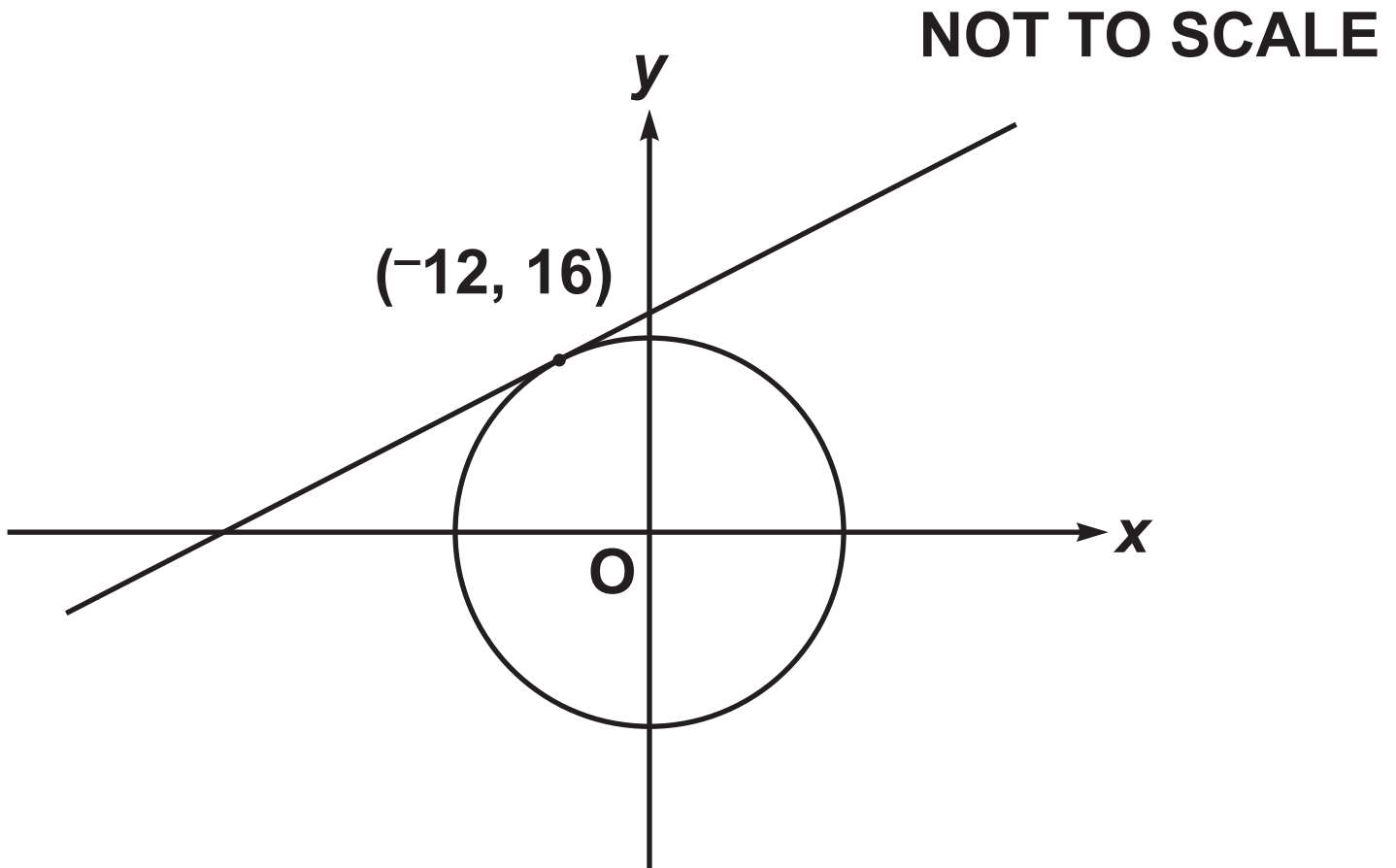
He then wants to paint his name on the trailer.

The name must be in a different colour to the trailer.

In how many different ways can Alfie paint his model lorry?

(b) _____ [3]

- 14 The diagram shows a circle with centre $(0, 0)$ and a tangent at the point $(-12, 16)$.



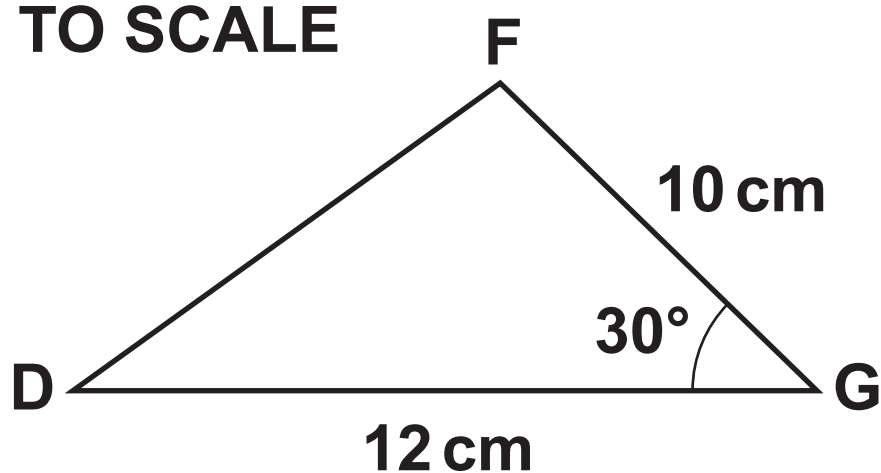
The tangent crosses the y -axis at the point $(0, p)$.

Find the value of p .

$$p = \underline{\hspace{2cm}} \quad [5]$$

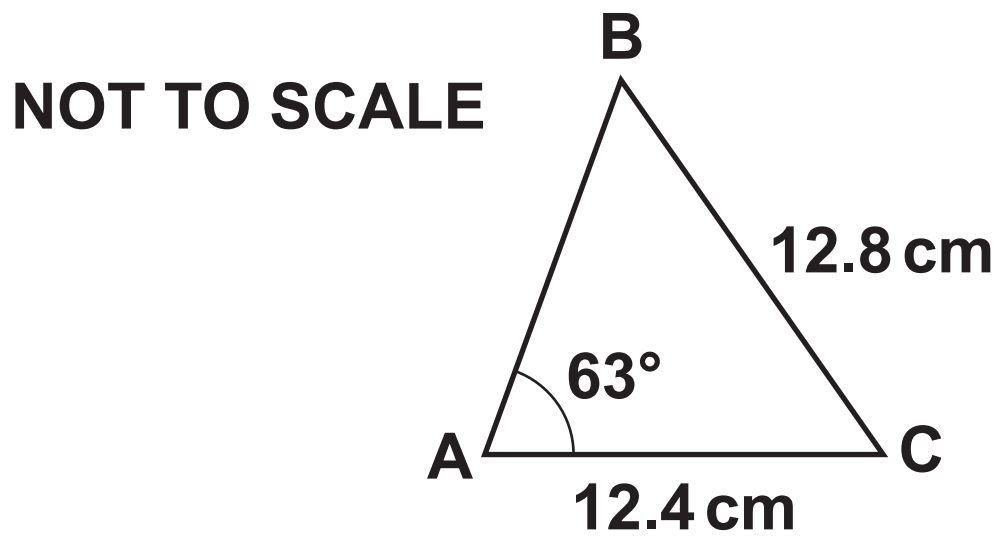
15 (a) Calculate length DF in this triangle.

NOT TO SCALE



(a) _____ cm [3]

(b) Calculate angle ACB in this triangle.

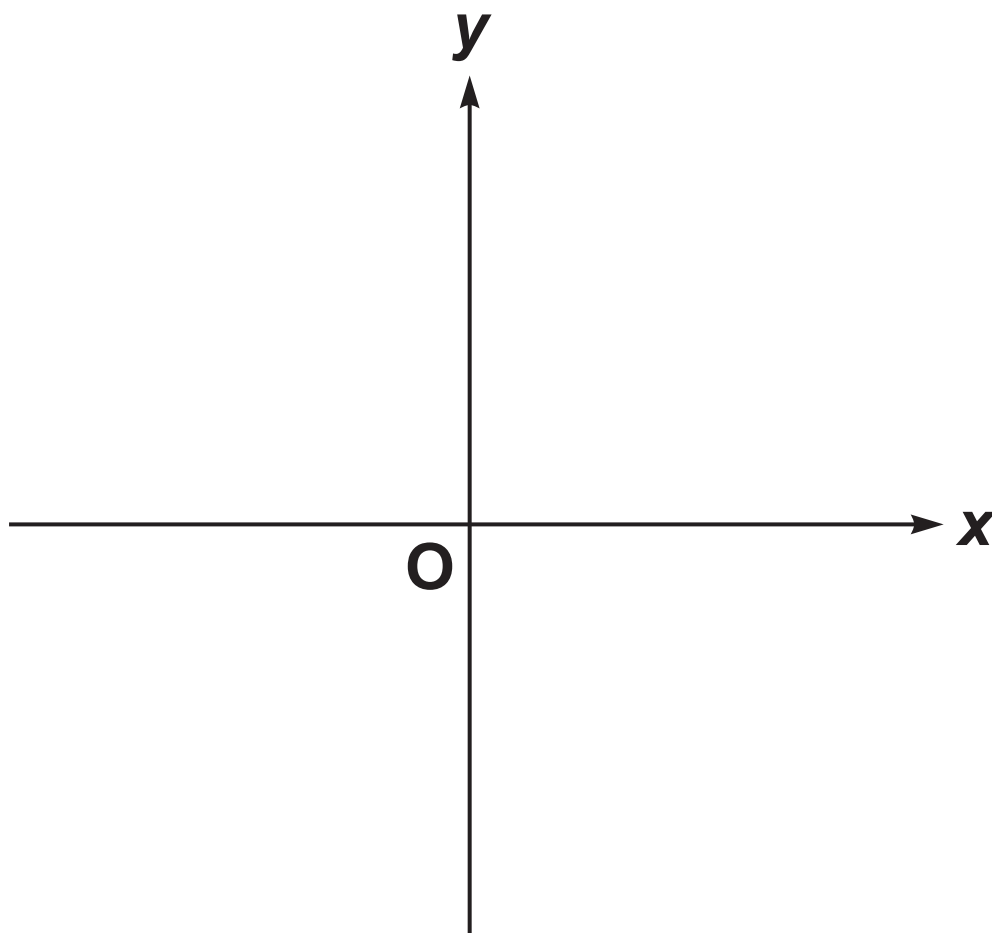


(b) _____ ° [4]

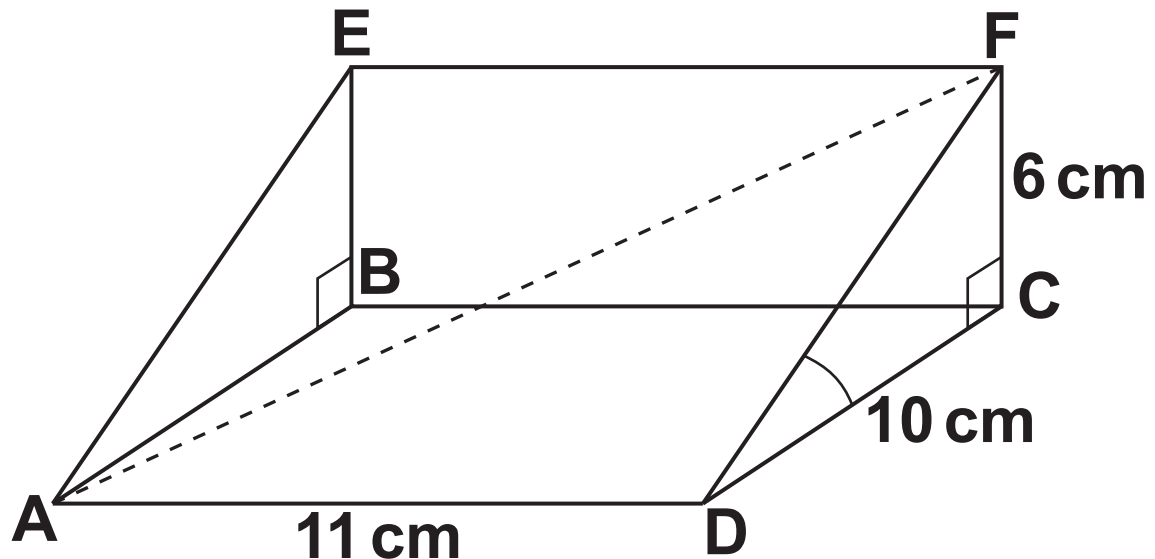
16 Show that $\frac{x+9}{x^2-1} + \frac{4}{x+1}$ can be written
in the form $\frac{a}{x-1}$, where a is an integer.

Use the space below. [4]

- 17 Sketch the graph of $y = 3^x$.
Give the value of the y -intercept. [2]**



- 18 The diagram shows a right-angled triangular prism $ABCDEF$. You may use a model to help you.



Length $AD = 11\text{ cm}$, length $CD = 10\text{ cm}$ and length $CF = 6\text{ cm}$.

(a) Calculate the volume of the prism.

(a) _____ cm^3 [2]

(b) Use trigonometry to show that angle $FDC = 31^\circ$, correct to the nearest degree. [2]

(c) Calculate the exact length of AF.

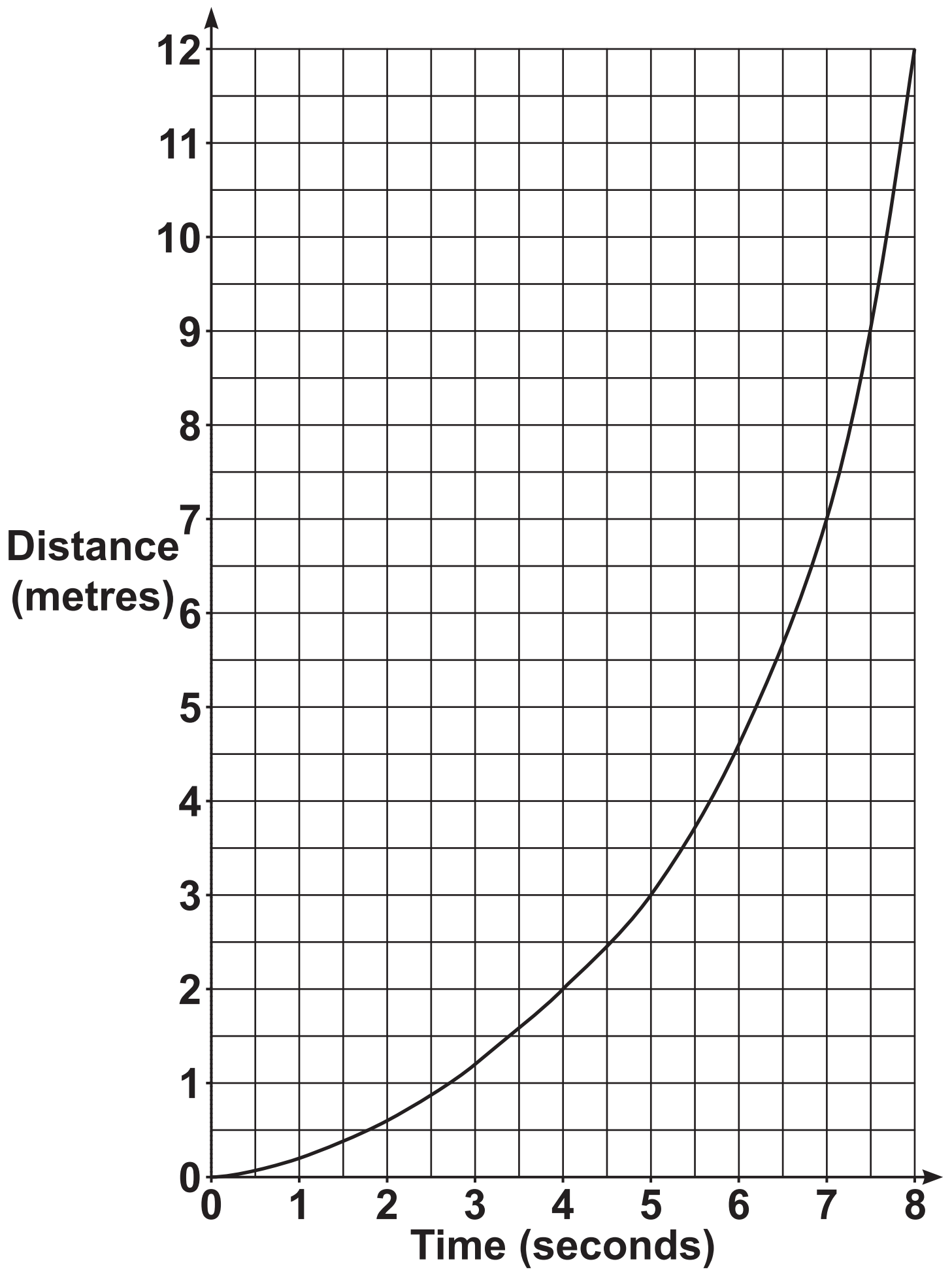
(c) _____ cm [4]

19 The graph opposite shows the distance travelled by a particle over 8 seconds.

Estimate the speed of the particle at 5 seconds.

_____ m/s [4]

END OF QUESTION PAPER



ADDITIONAL ANSWER SPACE

If additional space is required, you should use the following lined page(s). The question number(s) must be clearly shown in the margin(s).

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